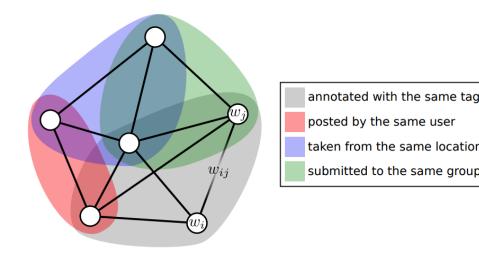
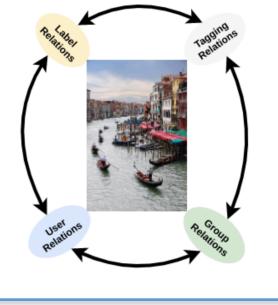
## Introduction

In a social network, the neighbourhood of an entity which can be image, post or user often carry sufficient information for tasks such as classification, recommendation or link prediction



## <u>Goal</u>

Learn one type of relations between entities to predict other type of relations in a social network



## **Challenges**

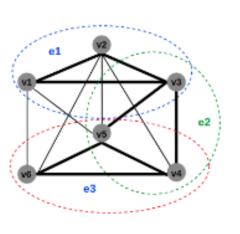
1.Representation - To avoid any loss in information

2.Information Flow - To transfer neighbourhood features across entities

3.Generalizability - To cover all kinds of social networks



Hypergraph is a generalisation of a graph in which an edge can connect any number of vertices.



Matrix Completion (Candès et al. 2008)

 $\min$ 

 $\mathbf{X} \in \mathbb{R}^{m imes n}$ 

$$\min_{\mathbf{X}\in\mathbb{R}^{m\times n}} \|\mathbf{X}\|_* + \underbrace{\mu\|\boldsymbol{\varOmega}\circ(\mathbf{X}-\mathbf{A})}_{\mathbf{X}\in\mathbb{R}^{m\times n}}$$

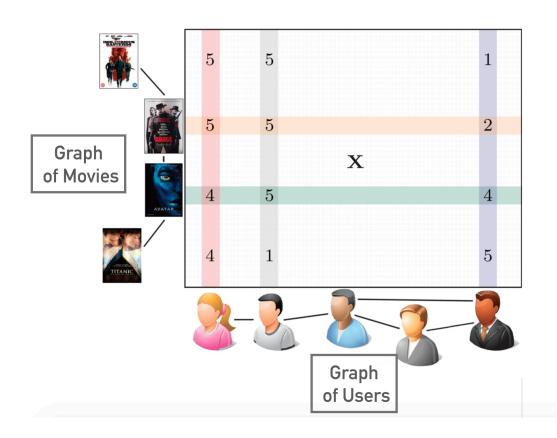
 $L(\mathbf{X})$ Geometric Matrix Completion (Kalofolias et al. 2014)

$$\mu(\mathbf{X}) + \mu_{c} \underbrace{\operatorname{tr}(\mathbf{X}\boldsymbol{\Delta}_{c}\mathbf{X}^{\top})}_{\parallel \mathbf{X} \parallel^{2}} + \mu_{r} \underbrace{\operatorname{tr}(\mathbf{X}^{\top}\boldsymbol{\Delta}_{r}\mathbf{X})}_{\parallel \mathbf{X} \parallel^{2}}$$

 $\|\mathbf{A}\|_{\mathcal{G}_{\mathcal{C}}}$  $\|\mathbf{A}\|_{\mathcal{G}_r}$ with  $\boldsymbol{\Delta}_{\mathrm{r}}, \boldsymbol{\Delta}_{\mathrm{c}}$  the row and column graph laplacians.

Multi- Graph Convolutional Neural Networks (MGCNN)<sup>[2]</sup> A multi-graph convolution can be obtained as:  $\mathbf{X}\star\mathbf{Y}=oldsymbol{\varPhi}_{\mathrm{r}}(\hat{\mathbf{X}}\circ\hat{\mathbf{Y}})oldsymbol{\varPhi}_{\mathrm{c}}^{ op}.$ 

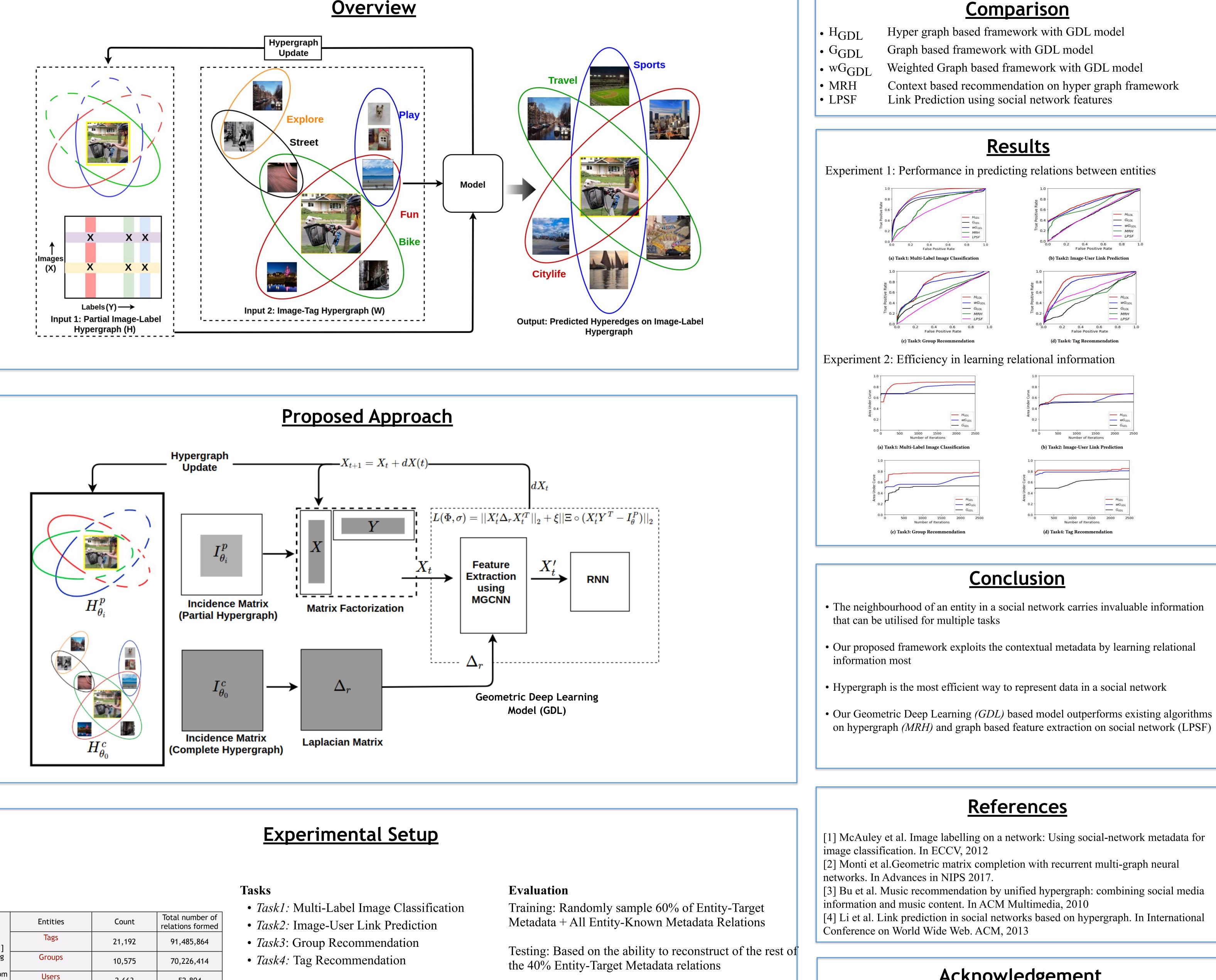
which simplifies matrix completion problem on graphs to minimising  $\ell(\boldsymbol{\Theta}) = \|\mathbf{X}_{\boldsymbol{\Theta}}^{(T)}\|_{\mathcal{G}_r}^2 + \|\mathbf{X}_{\boldsymbol{\Theta}}^{(T)}\|_{\mathcal{G}_c}^2 + \mu L(\mathbf{X}_{\boldsymbol{\Theta}}^{(T)})$ 

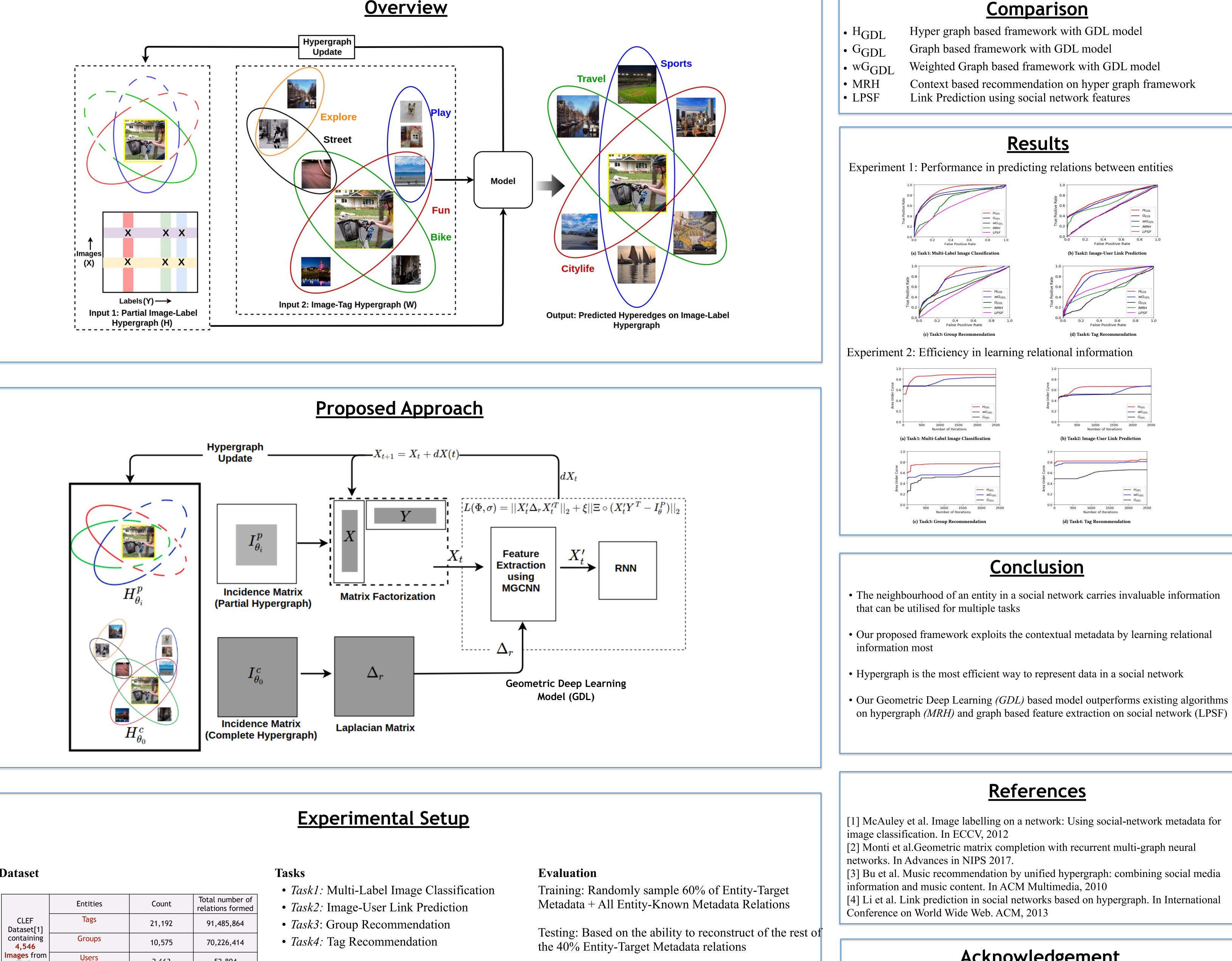


## Exploiting Relational Information in Social Networks using Geometric Deep Learning on Hypergraphs

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### Dataset

| CLEF<br>Dataset[1]<br>containing<br><b>4,546</b><br>Images from<br>Flickr | Entities | Count  | Total number of relations formed |
|---|----------|--------|----------------------------------|
|   | Tags     | 21,192 | 91,485,864                       |
|   | Groups   | 10,575 | 70,226,414                       |
|   | Users    | 2,663  | 52,804                           |
|   | Labels   | 99     | 613,014                          |



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### Acknowledgement

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 700381

